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PRELIMINARY DATA ON BUCKLING STRENGTH OF

CURVED SHEET PANELS IN COMPRESSION

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PRELIMINARY DATA ON BUCKLING STRENGTH OF

CURVED SHEET PANELS IN COMPRESSION

By Eugeno E. Lundquist -

SUMMARY

This paper presents the results obtained in compression tests of eight stiffened panels. The radius-thickness ratio of the skin between stiffeners varied from 400 to infinity.

From those few tests, it is concluded that the critical compressive stress for a curved sheet between stiffeners is equal to the larger of the following:

- (a) The critical coupressive stress for an unstiffened circular cylinder of the same radius-thickness ratio
- (b) The critical compressive stress for the same sheet when flat

INTRODUCTION

In the design of airplane structures, it is desirable to know the effect of curvature on the strongth of the thin netal skin. A number of years ago, the NACA undertook the investigation of the strength of thin-walled duralumin cylinders. The cylinders were tested in a variety of leading conditions, and in all cases failure occurred through instability of the cylinder walls. One of the conditions of leading was that of axial compression. The results of these compression tests are given in reference 1.

As an extension of the cylinder investigation, it was decided to study the critical buckling load for thin curved sheets between stiffeners. The purpose of this report is to present the results of the tests on the first group of specimens in this new investigation.

Ivar C. Peterson, formerly of the NACA staff, performed the experimental work in this investigation.

HATERIALS ,

The material used in this investigation was 24S-T aluminum alloy. As all specimens were leaded within the elastic range of the material, the modulus of elasticity. E, is the only material property of concern. This value was assumed to be 10,600,000 pounds per square inch in all the calculations of this paper.

SPECIMENS AND THEIR DESIGNATION

The specimens tested in this investigation were made as shown in figure 1. The width of the outstanding flange of each stiffener at the side edges of the sheet, $b_{\rm F}$, is given in table I. The different values of $b_{\rm F}$ were selected so as to force buckling to occur in the sheet between stiffeners and still provide as much support as possible against deflection normal to the sheet.

The angle type of stiffener was selected because of the low rotational restraint that it provided at the side edges of the sheet. The use of two stiffeners at each side edge of the sheet was decided upon in order to stabilize thoroughly these edges against displacements normal to the sheet.

All specimens are designated by their radius—thickness ratio, r/t. In some cases more than one test was made on a given specimen. Thus, the designation of a test is the radius—thickness ratio of the specimen, followed by the number of the test on that specimen. For example, test No. 1318—1 represents the first test on the specimen with r/t = 1318.

In all calculations of stress in this report the areas used were determined from the weight of the specimens. Hence all the dimensions given on figure 1 should be regarded as nominal.

APPARATUS AND METHOD

All specimens were tested in a 300,000-pound compression testing machine. Strains were measured by Tuckerman

optical strain gages of 2-inch gage length on the front and back side of the sheet at each of the locations shown in figure 1. The loading heads of the machine were as-justed so as to bear uniformly on the specimen as indicated by strain gages. As the ends of the specimen had been carefully machined flat, this method of testing was practical although it did take seme time to adjust the loading heads of the machine.

No reliable deflection readings were taken in the tests. It was reasoned that the difference in the strain readings on front and back of the sheet was an accurate measure of the change in curvature. According to the theory of small deflections, which applies for all stresses up to the buckling lead, the deflection for a given buckled shape is proportional to the curvature. It was considered that the strain readings of the Tuckerman optical strain gages were more accurate than the deflection readings that could be obtained with the equipment at hand.

DETERMINATION OF CRITICAL BUCKLING LOAD

Of the eight specimens tested, those with high curvatures buckled suddenly by a snap diaphragm action, accorpanied by a loud report. These having r/t = & and 1318 did not give such a clearly defined critical buckling point. For these latter specimens, there was a gradual growth of deflection that made visual detection of the critical load impossible. In order to obtain the critical buckling load for these two specimens, resort was made to the nethods of analyzing experimental observations in problems of elastic stability as given in reference 2. This nethod is an analysis of the growth of deflection with load and consists of plotting (y-y₁)/(P-P₁) as ordinate against (y-y₁) as abscissa

whore

- P and y load and corresponding doflection, respectively
- P₁ and y₁ initial values of P and y, respectively

The inverse slope of the straight line obtained is $(P_{cr} - P_{r})$.

The results of the foregoing type of analysis as applied to the specimen with $r/t = \infty$ and 1318 are given in tables II to V, inclusive, and in figure 2. In this application the symbol y is the difference in strain readings between the two strain gages at the center of the shoot.

RESULTS

The results of these tests are given in table VI and figures 3 and 4. Figure 3 has been propared to show how the strains at the middle of the sheet varied below the critical buckling leads. It is observed from figure 3 that in each test the two strain gages on the front and back of the sheet reveal a gradually increasing difference of strain as the critical lead is approached. For the specimens with $r/t = \infty$ and 1318, the gradual increase in the difference of strain continued through the critical lead, whereas for all other specimens there was an abrupt change in the strain readings at the critical lead caused by the snap diaphragm action. As the intensity or force of the snap diaphragm action increased with increasing curvature, the strain gages were removed just before the buckling lead was reached in the case of the specimens with r/t = 478, 452, and 400.

In order to study the effect of the radius-thickness ratio, r/t, on the critical strain, $f_{\rm cr}/E$, figure 4 was propared. The lines labeled A, B, and C on this figure are the same as lines A, B, and C in figures 7 and 9 of reference 1. The horizontal lines labeled $r/t=\infty$ in figure 4 give the experimentally determined critical strain for the flat specimen of this investigation. The points plotted on figure 4 give the observed critical strain on the remainder of the specimens with each point plotted at the r/t value for the particular specimen represented by that point.

From the test data plotted in figures 7 and 9 of reference 1, it is clear that line B in figure 4 of this paper gives the upper limit of the experimentally deternined values of $f_{\rm cr}/E$ for thin-walled cylinders without longitudinal stiffeners. The fact that the test points in figure 4 plot along line B and the horizontal lines labeled $r/t = \infty$, indicates that the critical compressive stress for a curved sheet between stiffeners is equal to the larger of the following:

- (a) The critical compressive stress for an unstiffened circular cylinder of the same radius-thickness ratio
- (b) The critical compressive stress for the same sheet when flat

When these tests were planned it was expected to find that in all cases curvature would raise the critical compressive stress over that for the flat specimen r/t = ∞. (See equation (276), p. 470, of reference 3.) Why the experimental point for the specimen with r/t = 806 fails to check standard theory in this respect (see fig. 4) has not yet been explained. Additional tests are being made in the course of a further study of this point.

COUCLUSIONS

Fron those few tests, it is concluded that the critical compressive stress for a curved sheet between stiffeners is equal to the larger of the following:

- (a) The critical coupressive stress for an unstiffened circular cylinder of the same radiustickness ratio
- (b) The critical compressive stress for the same shoot when flat

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TABLE II. - TEST 00 -1

(1b)	(in.)	P-P ₁ (1b)	y-y ₁ (in:)	y-y ₁ P-P ₁ (in./lb)
200 1000 2000 3000 4000 5000 6000 6500 7000	0 .000002 .000004 .000008 .000016 .000032 .000060 .000094 .000142	800 1800 2800 3800 4800 5800 6300 6800	0 .000002 .000008 .000016 .000032 .000060 .00094	-0.2500×10 ⁻⁸ .2222 .2857 .4211 .6667 1.0345 1.4921 2.0882

TABLE III.- TEST 00 -2

(1b)	(in.)	P-P ₁ (1b)	y-y ₁ (in.)	y-y ₁ P-P ₁ (in./lb)
200 1000 2000 3000 4000 5000 6000 6500 7000 7250	0 .000002 .000004 .000014 .000012 .000022 .000030 .000046 .000072 .000132	0 800 1800 2800 3800 4800 5300 5300 6300 6800 7050	0 .000002 .000004 .000012 .000022 .000030 .000046 .000072 .000112	-0.2500×10 ⁻⁸ .2222 .1429 .3158 .4583 .5660 .7931 1.1429 1.6471 1.8723

TABLE IV. - TEST ∞ -3

(1b)	y (in.)	P-P ₁ (1b)	y-y ₁ (in ₄)	y-y ₁ P-P ₁ (in./1b)
500 1000 2000 3000 4000 4500 5500 6500 6500 6750 7000	0 .000020 .000018 .000020 .000026 .000036 .000036 .000070 .000108 .000126 .000154	0 500 1500 2500 3500 4000 4500 5000 6250 6500	0 .000020 .000018 .000020 .000026 .000032 .000036 .000018 .000126 .000126	- 4.000×10-8 1.200 .800 .743 .800 .800 .960 1.273 1.800 2.369

TABLE I .- DIMENSIONS OF SPECIMENS

Ŧ	Radius of sheet (in.)	Outstanding flange of angle stiffener, by (in.)
∞ 1318 806 634 542 478 432 400	00 103.0 63.5 49.2 37.3 33.8 31.1	1.51 1.51 1.08 1.08 1.08 .87 .75

TABLE V.- TEST 1318-1

) (1b)	y (in.)	P-P1 (1b)	y-y ₁ (in.)	y-y ₁ P-P ₁ (in _* /1b)
500 1000 2000 3000 4000 4500 5500 6000 6500 6750 7000 7 250	0 .000002 000002 .000012 .000018 .000026 .000026 .000040 .000068 .000086 .000110 .000142	0 500 1500 2500 3500 4500 4500 4500 6500 6250 6750	0 .000002 -000002 .000012 .000015 .000020 .000026 .000040 .000065 .000066	0.4000×10 ⁻⁸ 133345004500444452007273 1.1333 1.3750 1.6923 2.1037

TABLE VI.- TEST RESULTS (E = 10.6 × 10⁶)

Test	r t	Area, A (sq in.)	Buckling load, P (1b)	Buckling stress, for (lb/sq in.)	f _{or}
-1 -2 -2 -3 1318-1 806-1 634-1 634-2 542-1 478-1 432-1 400-1	∞ ∞ 1318 806 634 634 542 478 432 400	1.3100 1.3100 1.3100 1.3100 1.1578 1.1552 1.1552 1.1029 1.1020 1.0668	7,430 7,630 7,660 7,670 6,250 7,800 7,280 9,030 9,380 11,050	5,670 5,820 5,850 5,400 6,750 6,600 8,190 8,790 10,360	5.349×10 ⁻⁴ 5.491 5.519 5.519 6.36 5 6.226 6.226 7.726 8.292 9.774

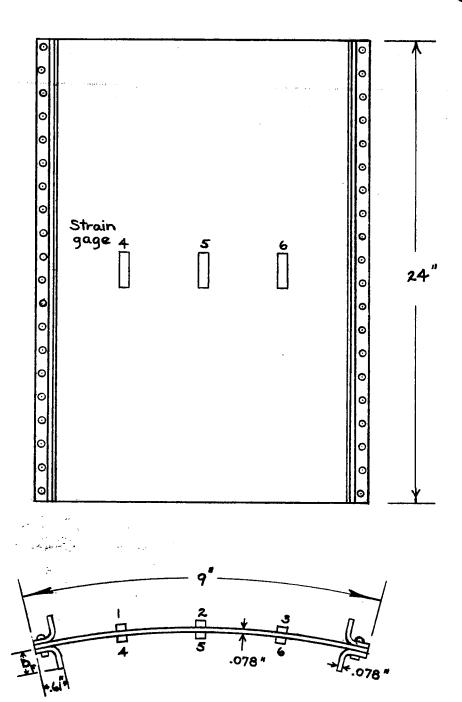
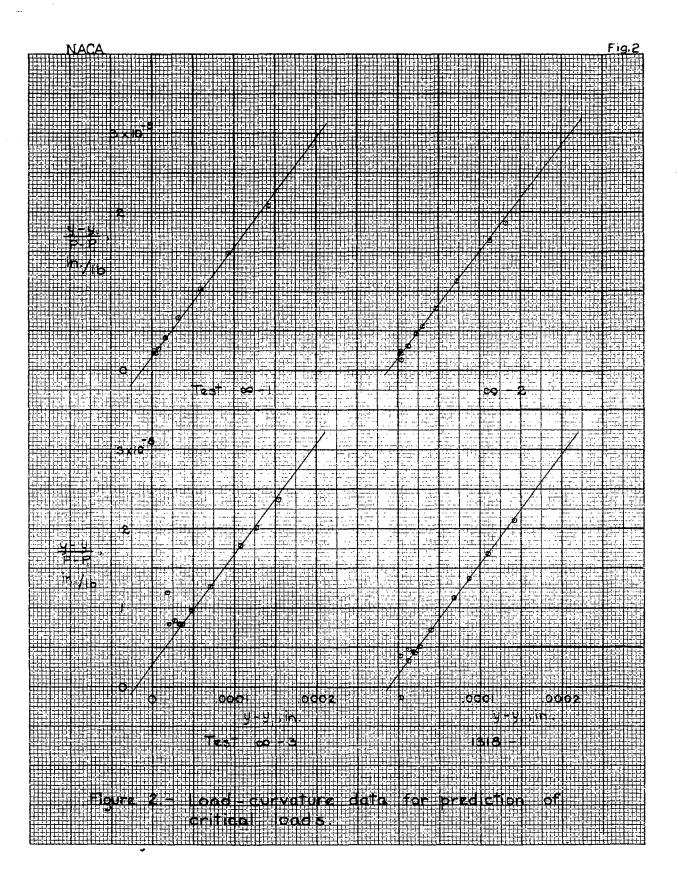
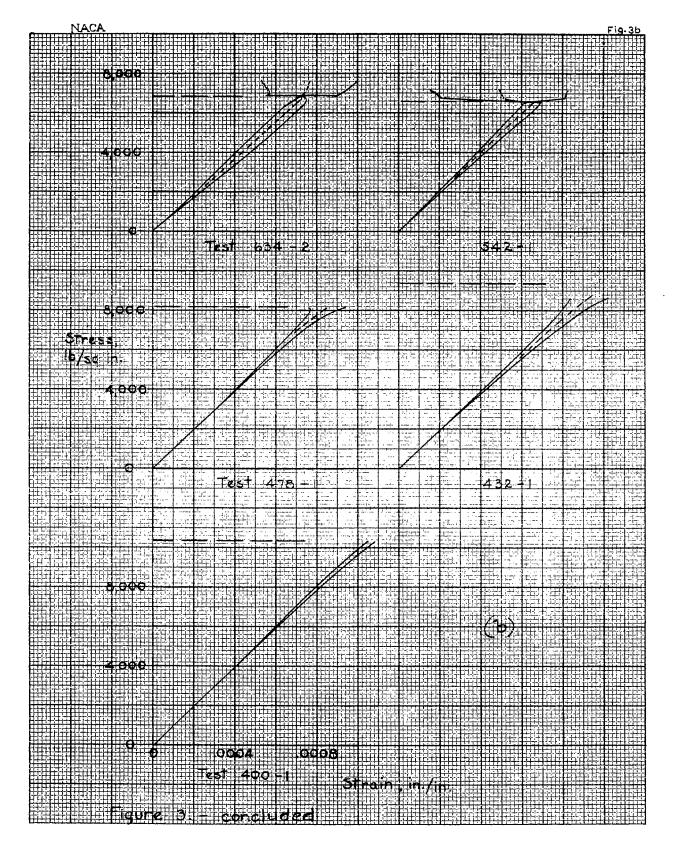
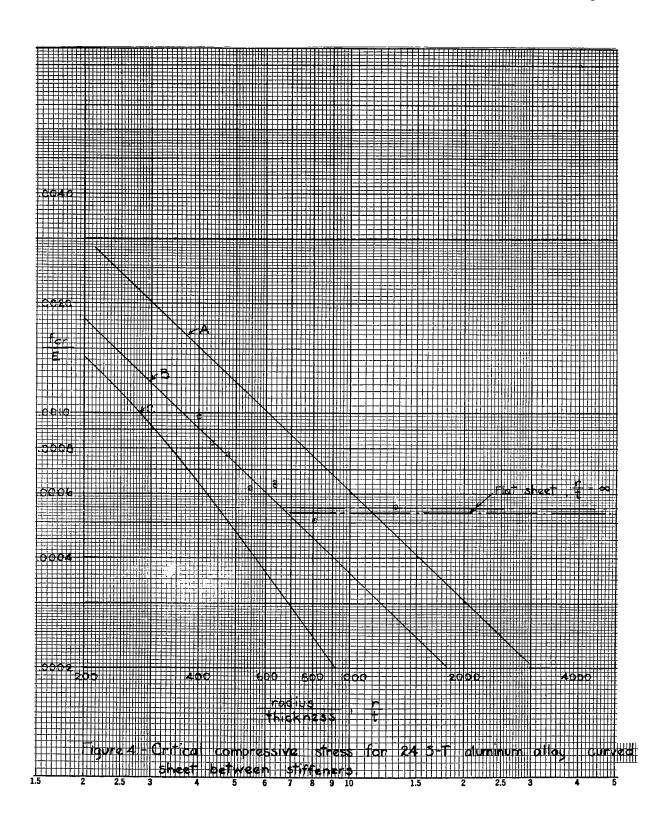


Figure 1. - Test specimen.



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3 1176 01403 6108